Radicals in classification of commutative reduced filial rings

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Abstract. A ring in which every accessible subring is an ideal is called filial. Let $\mathbb{S} = \left\{R : \forall_{x\in R}\ x \in Rx^2\right\}$ be the class of all strongly regular rings, $\mathbb{S}_a = \left\{R : \forall_{x\in R}\ \exists_{n\in\mathbb{N}}\ nx \in Rx^2\right\}$ be the class of all almost strongly regular rings and for a prime p let $\mathcal{T}_p = \{R : pR = R\}$. $\mathbb{S}$, $\mathbb{S}_a$, $\mathcal{T}_p$ are radical classes. The aim of the talk is to present properties and applications of above radicals in classification of commutative reduced filial rings.

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